

THE BINARY SORT ACCESS METHOD, US Patent 5,926,815:

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BSAM adds keys over 28% faster and reads keys in sorted order over 2% faster than optimized B*-tree methods.

Component	Compares			Moves	
	Stable	Average	Maximum	Average	Maximum
heap_sort	No	$n \log n$	$n \log n$	$n \log n$	$n \log n$
quick_sort	No	$n \log n$	n^2	$n \log n$	n^2
radix_sort	No	$n \log n$	n^2	$n \log n$	n^2
BSAM	Yes	$\left(\int (1 + \log_2(1 + (b * (0.5 * (\int((n-1)/b) * (\int((n-1)/b + 1)))))) + (((b^2) * (\int((n-1)/b) + (\text{mod}(n-1, b) + 1) * (1 + (1.5 * (\text{mod}(n-1, b)))) + (\int(1 + \log_2(1 + (b * (0.5 * (\int((n-1)/b) * (\int((n-1)/b + 1))))))))) \right) / 4) + (b * (\int((n-1)/b))) \right)$ where b is the number of blanks inserted, $\text{mod}(x, y) = x - y * \text{int}(x/y)$, log base two as $\lg(x) = \log(x) / \log(2)$, and see Sedgewick and Flajolet [1996]	$\left((b * (1 + (1.5 * (b - 1)))) * (\int((n-1)/b)) + (b * (\int((n-1)/b) + 1) * ((\int((n-1)/b) + 1) - 1) / 2) + (\text{mod}(n-1, b) + 1) * (1 + (1.5 * (\text{mod}(n-1, b)))) + (\int(1 + \log_2(1 + (b * (0.5 * (\int((n-1)/b) * (\int((n-1)/b + 1)))))) \right) / 4) + (b * (\int((n-1)/b))) \right)$ where b is the number of blanks inserted, $\text{mod}(x, y) = x - y * \text{int}(x/y)$, and log base two as $\lg(x) = \log(x) / \log(2)$	$\left((b * (b - 1) / 2) * (\int((n-1)/b)) + (b * (\int((n-1)/b) + 1) * ((\int((n-1)/b) + 1) - 1) / 2) + (\text{mod}((n-1), (b) + 1) * ((\text{mod}((n-1), (b) + 1) - 1) / 2)) \right)$ where $\text{mod}(x, y) = x - y * \text{int}(x/y)$ and b is the number of blanks inserted	

Contrast of worst performance for compares and moves of quick sort or radix sort (n^2) and BSAM.

Compares				Moves			
n	n^2	BSAM	Times_fewer	n	n^2	BSAM	Times_fewer
100	10^4	2 089	4.79	100	10^4	990	10.10
1 000	10^6	61 046	16.39	1 000	10^6	50 040	19.98
10 000	10^8	4 709 553	21.23	10 000	10^8	4 599 540	21.74
100 000	10^{10}	456 104 559	21.92	100 000	10^{10}	455 004 540	21.98
1 000 000	10^{12}	45 470 954 566	21.99	1 000 000	10^{12}	45 459 954 540	22.00
10 000 000	10^{14}	4.5456105e+12	22.00	10 000 000	10^{14}	4.54555005e+12	22.00
100 000 000	10^{16}	4.545471e+14	22.00	100 000 000	10^{16}	4.54546e+14	22.00
1 000 000 000	10^{18}	4.5454561e+16	22.00	1 000 000 000	10^{18}	4.545455e+16	22.00

Contrast of average performance for compares and moves of quick sort or radix sort ($n \lg n [+ n]$) and BSAM.

Compares				Moves			
n	$n \lg n [+ n]$	BSAM	Times_fewer	n	$n \lg n [+ n]$	BSAM	Times_fewer
100	764	381	2.01	100	764	372	2.05
1 000	10 966	3 754	2.92	1 000	10 966	3 738	2.93
10 000	142 877	37 520	3.81	10 000	142 877	37 497	3.81
100 000	1 760 964	375 017	4.70	100 000	1 760 964	374 988	4.70
1 000 000	20 931 569	3 750 033	5.58	1 000 000	20 931 569	3 749 997	5.58
10 000 000	2.4253497e+8	37 500 030	6.47	10 000 000	2.4253497e+8	37 499 987	6.47
100 000 000	2.7575425e+9	3.75e+8	7.35	100 000 000	2.7575425e+9	3.75e+8	7.35
1 000 000 000	3.0897353e+10	3.75e+9	8.24	1 000 000 000	3.0897353e+10	3.75e+9	8.24

Graph of performance contrasting B*-tree and BSAM.

